

# Multi-User Quantum Communication Networks

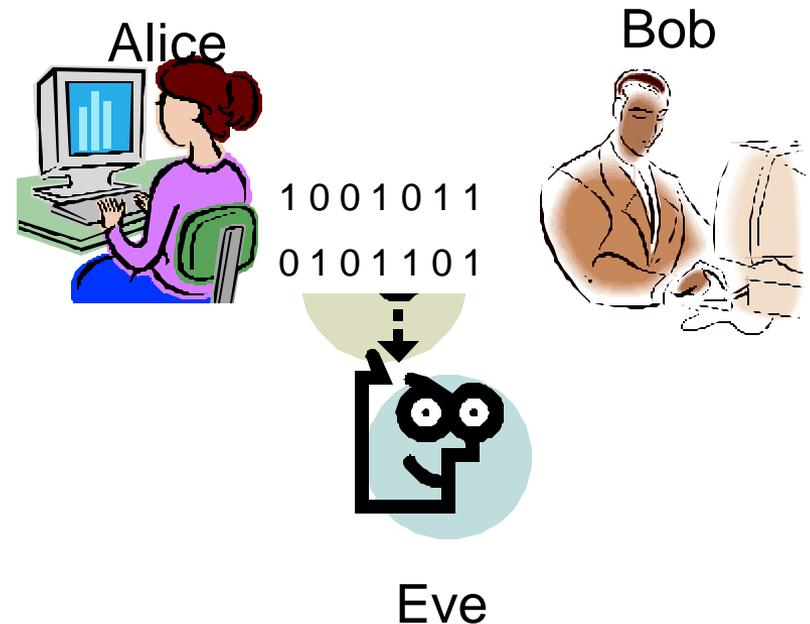
**Bing Wang, Patrick Kumavor, Craig Beal,  
Susanne Yelin\***

**Electrical & Computer Engineering Department, University of  
Connecticut, Storrs, CT 06269**

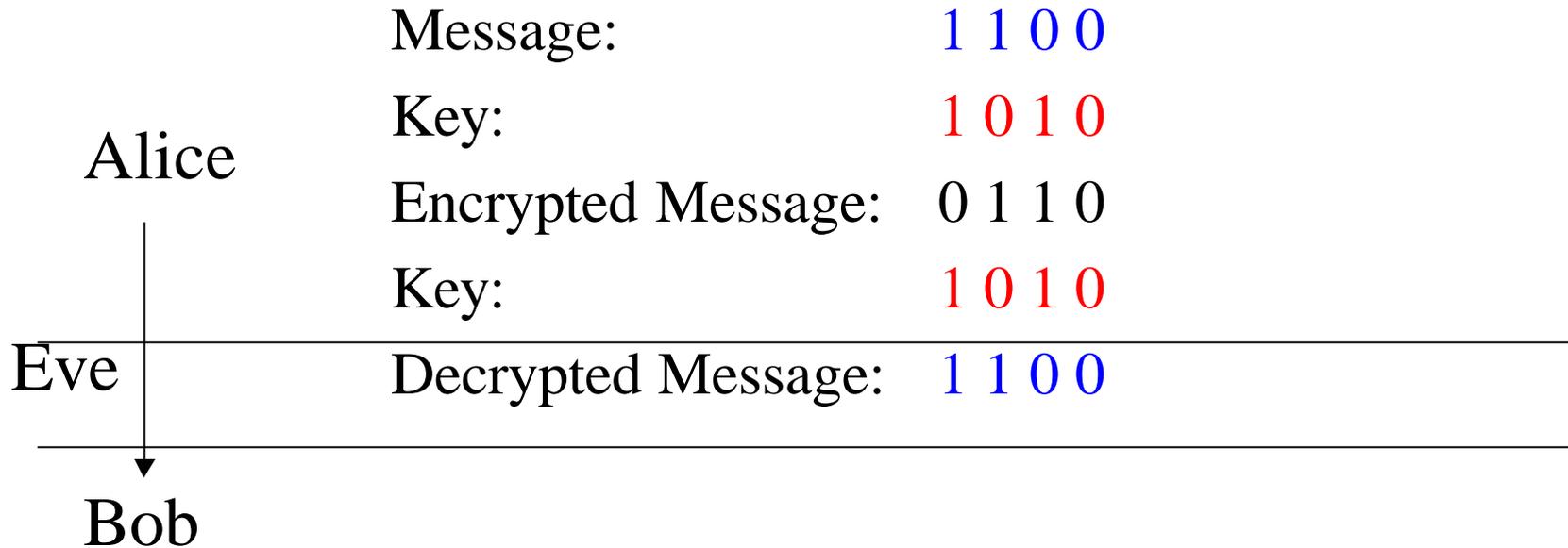
**\*Physics Department, University of Connecticut**

# Quantum Key Distribution

- Traditional 128bit (mathematical) public key encryption are highly susceptible to decryption by powerful computers
- Perfect Encryption is possible with Vernam Cipher, (aka One Time Pad)
- Quantum Key Distribution: Secure distribution of encryption keys possible using quantum bits, or Qubits
- Security of QKD is independent of computing power.
- Security of QKD based on fundamental Quantum Mechanical principles: the uncertainty principle and the no-cloning theorem.
- Any attempt to eavesdrop will be immediately detected.



# Encryption

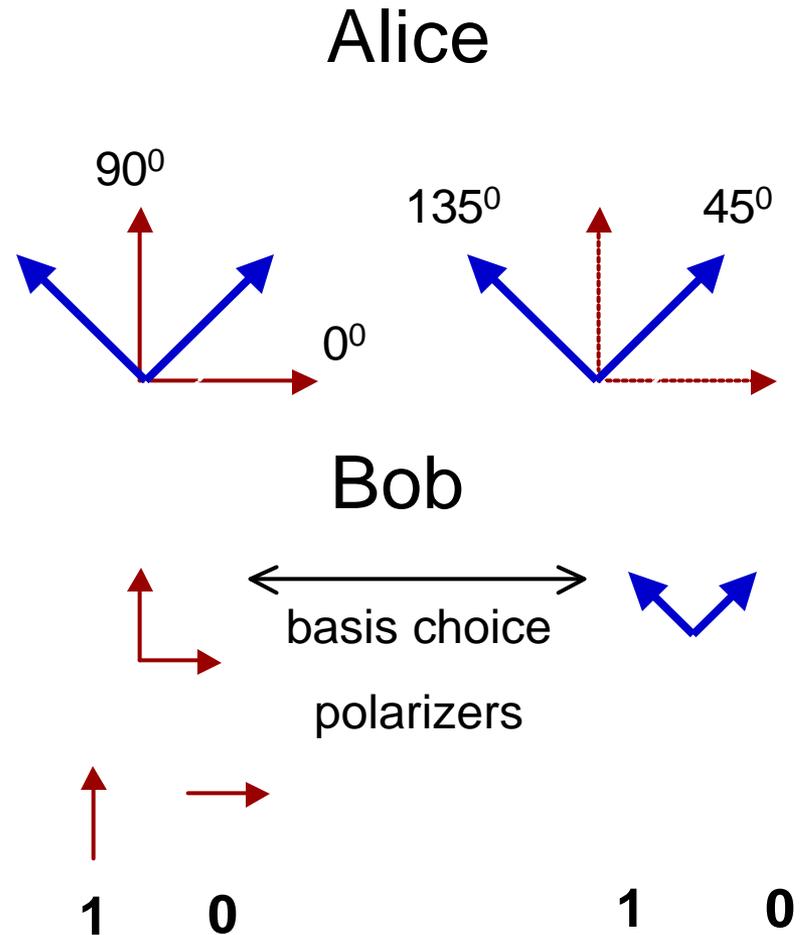


If key only used ONCE (One Time Pad), then encryption is secure, but.....

Problem of Key Distribution

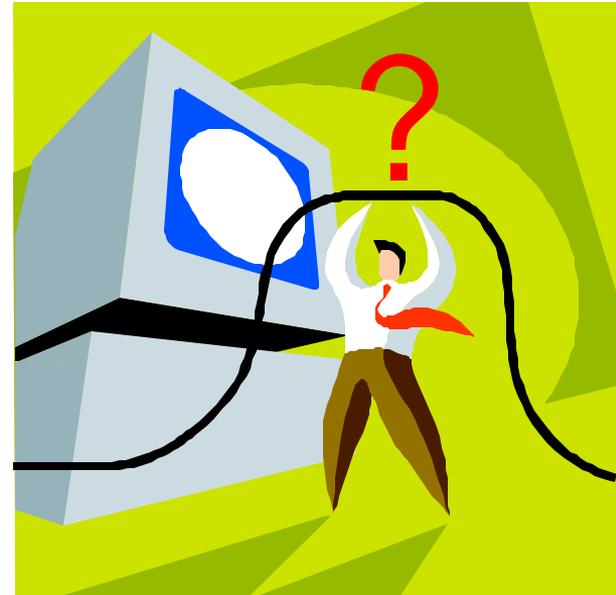
# Quantum Key Distribution

- QKD transmits photon in two non-orthogonal basis sets, such as Polarization or Phase
- Polarization: “Alice” transmits in  $[0,1]$  in 1<sup>st</sup> basis as  $0^\circ$  &  $90^\circ$  and  $[0,1]$  in 2<sup>nd</sup> basis as  $45^\circ$  &  $135^\circ$
- “Bob” chooses the between the two basis randomly. Bob’s choice will coincide with Alice’s in 50% of the time
- After photons are sent, Alice and Bob communicate over public channel on which basis was used.
- Bob keeps qubits detected using same basis



# Quantum Key Distribution

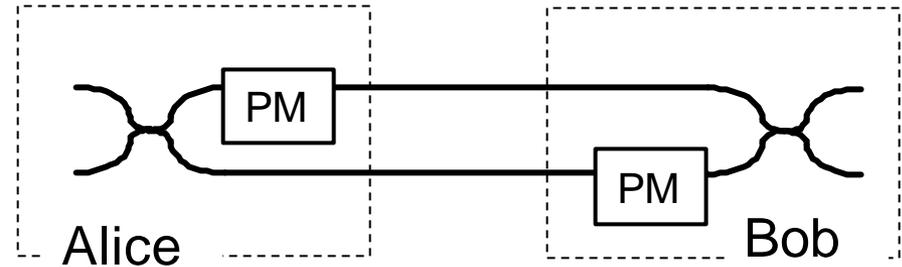
- ✦ !! Alice does NOT send quantum encryption key to Bob !!
- ✦ The key is created when Bob and Alice decides on their basis choice AFTER the qubit photons are transmitted.
- ✦ Eavesdropper Eve cannot know which basis to use because it's decided AFTER transmission.
- ✦ If Eve taps the channel, the quantum bit error rate, or QBER, will increase significantly, alerting Alice and Bob of Eve's presence.
- ✦ Phase encoded QKD uses interferometer instead of polarized light and polarizers



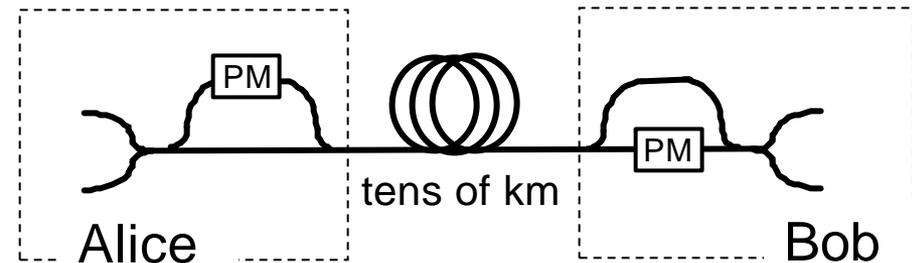
# Phase Encoded QKD

- Phase encoded QKD uses interferometers
- Phase encoded QKD more practical in optical fiber systems due to polarization mode dispersion (PMD) in fiber.
- First demonstrated using a collapsed Mach-Zehnder optical fiber interferometer

Mach-Zehnder Interferometer



Collapsed Mach-Zehnder Interferometer



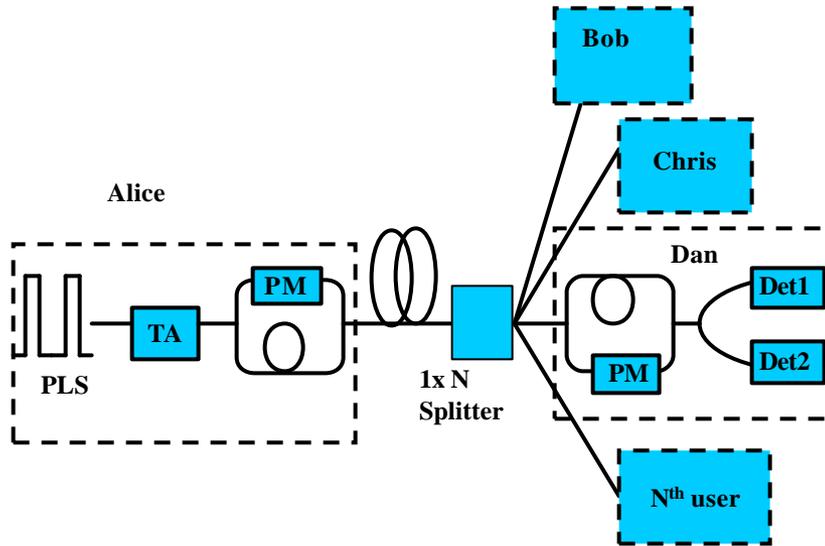
# Current efforts in quantum key distribution

- ✦ Present QKD research focuses on
  - ✦ New quantum protocols
  - ✦ Free-space implementation
  - ✦ Compatibility with existing state-of-the-art optical network communication technologies
- ✦ Current efforts include
  - ✦ Research groups: University of Geneva, Los Alamos National Lab, IBM research, Northwestern University
  - ✦ Start-up companies: MagiQ Technologies Inc, id-Quantique
  - ✦ Telcordia Technologies (working with Los Alamos), focuses on having 1.3mm quantum channels and 1.55mm classical optical communications on same fiber
  - ✦ BBN Technologies (Darpa funded), has multi-user testbeds, linking Harvard, Boston University, and BBN
  - ✦ *Special section at OFC 2005 dedicated to Quantum Information.*
  - ✦ *Our work published in Jan 05 issue of Journal of Lightwave Technology*

# QKD with network topologies

- ✦ Network topologies to be compared are
  - ✦ Passive star
  - ✦ Optical ring based on Sagnac interferometer
  - ✦ Wavelength-routed
  - ✦ Wavelength-addressed bus
- ✦ Single photon source approximated by highly attenuated coherent laser light
- ✦ Single photon detectors are avalanche photodiodes that are gated and operating in Geiger mode
- ✦ Alice encodes the transmitted photons using her phase modulator
- ✦ Bob measures photons with his phase modulator and single photon detectors
  - ✦ He assigns each detector with a bit value (0 or 1)
  - ✦ Knowing the phase shift he applies, he can infer from the detector that fired the phase shift and consequently the bit value Alice sent

# Passive star network topology

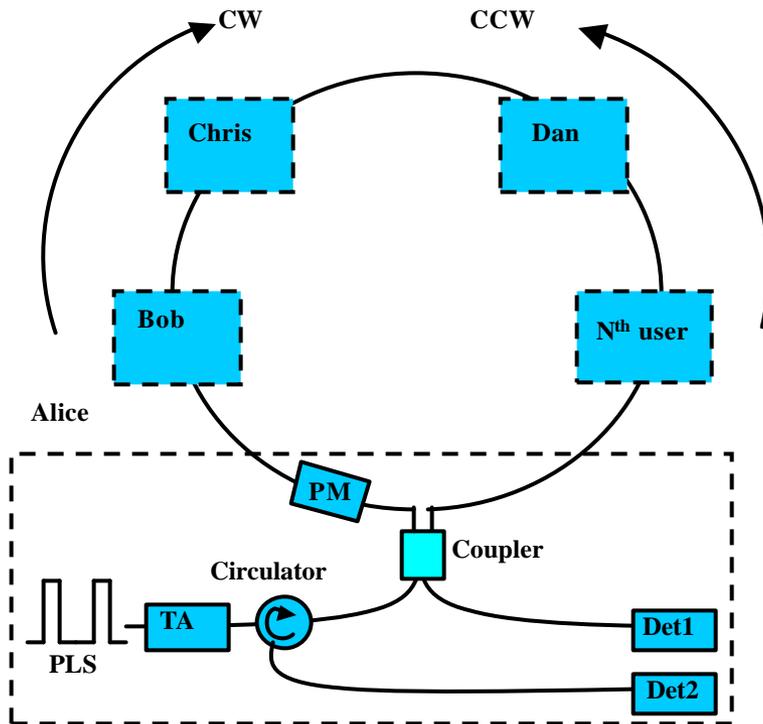


PLS- Pulsed laser source  
PM- Phase modulator  
TA- Tunable attenuator  
Det- Detector

- Passive star network connecting four users first demonstrated by Townsend [2]
- Alice equipped with PLS, TA, and PM
- Each end-user equipped with PM and two Det
- Alice is linked to other users via a 1xN splitter
- Photons are randomly routed to one user at a time since they are indivisible
- “Distance” is defined as the total fiber length spanning Alice and any of the users

[2] P.D Townsend, Nature, 385, 47, (1997)

# Optical ring network topology

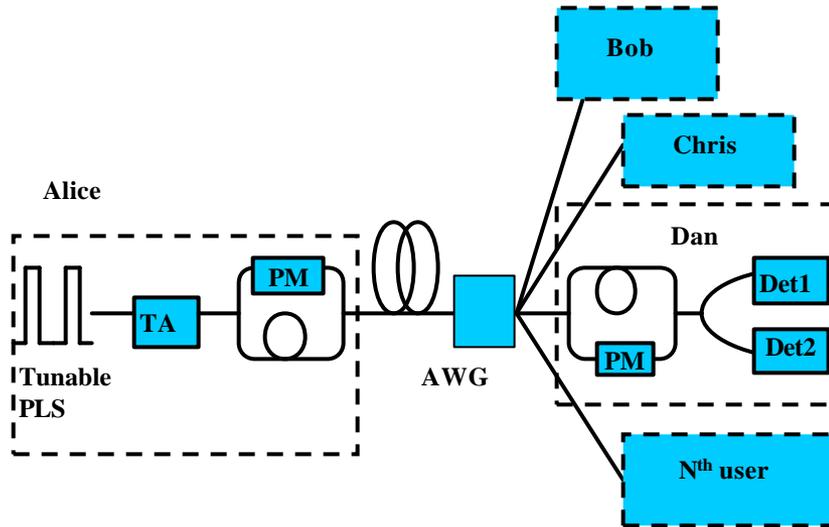


PLS- Pulsed laser source  
PM- Phase modulator  
TA- Tunable attenuator  
Det- Detector  
cw (ccw)-clockwise (counter clockwise)

- A two-user QKD system based on optical fiber Sagnac interferometer has been demonstrated by Nishioka et al. [3]
- Alice has PLS, TA, circulator, coupler, and PM
- Each end-user equipped with a PM
- Alice's circulator directs photons to the fiber loop and they traverse in both the cw and ccw directions
- Upon exiting loop, photons that take left turn are directed by circulator to Det2; those that take right go to Det1
- There is a control mechanism so that only one user can modulate photon at a time
- "Distance" is defined as the length of fiber loop

[3] T. Nishioka, H. Ishizuka, T. Hasegawa, and J. Abe, *IEEE Photonics Technology Letters*, 14, 576 (2002)

# Wavelength-routed network topology



PLS- Pulsed laser source

PM- Phase modulator

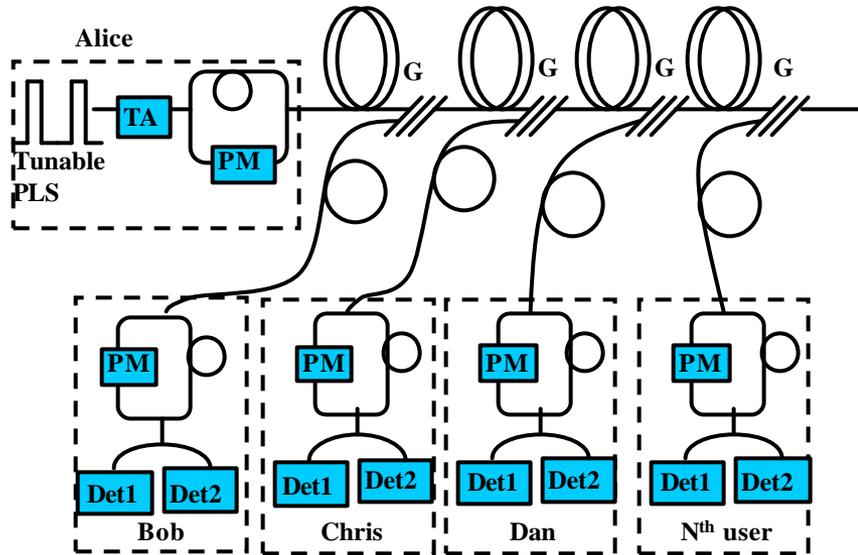
TA- Tunable attenuator

Det- Detector

AWG- Arrayed waveguide grating

- Alice's end consists of wavelength-tunable PLS, TA, and PM
- Each end-user has PM and two Det
- Network users each apporioned a separate wavelength channel
- Alice communicates with users via the AWG by tuning her laser to the corresponding wavelength
- "Distance is defined as the total fiber length spanning Alice and any user

# Wavelength-addressed bus network



PLS- Pulsed laser source  
PM- Phase modulator  
TA- Tunable attenuator  
Det- Detector  
G- Fiber bragg grating

- Alice's end is made up of tunable PLS, TA, and PM
- End-users each have PM and two Det
- Every user assigned a separate wavelength channel
- Each G is designed to match the wavelength of each user and reflects photons with wavelength corresponding to intended recipient, but otherwise transmits it
- Alice communicates with a particular user by tuning her laser to the wavelength designated for that user and sending the photon
- "Distance" is defined as total fiber length between Alice's and the end-users' ends

# Quantum bit error rate (QBER)

## Quantum bit error rate (QBER)

$$QBER = \frac{mThP_{opt} + P_{dark}}{mTh + 2P_{dark}}$$

$m$  - mean photon number

$T$  - transmission coefficient of link

$h$  - detector efficiency

$P_{opt}$  - probability of photon going to wrong detector

$P_{dark}$  - dark count probability

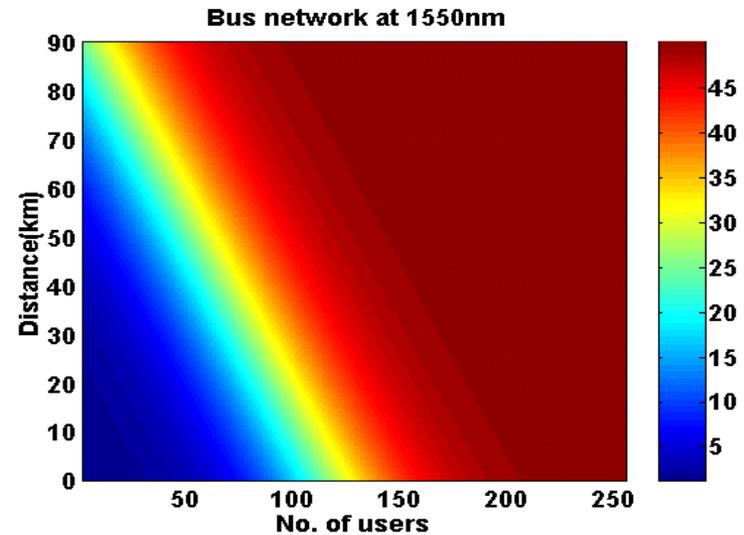
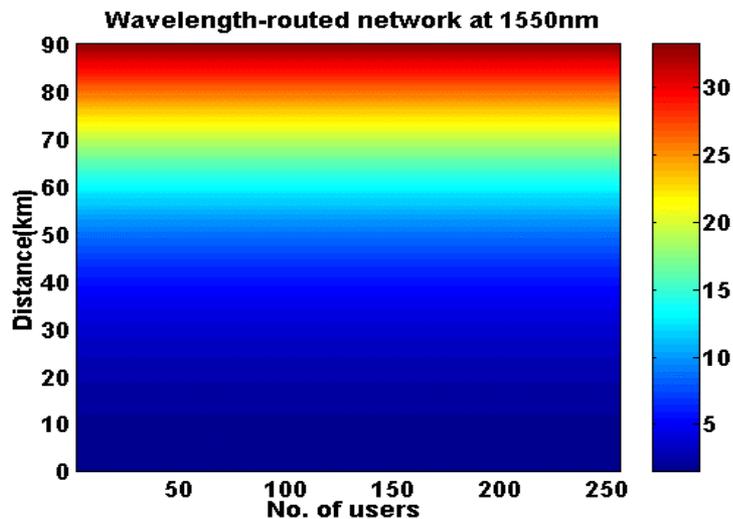
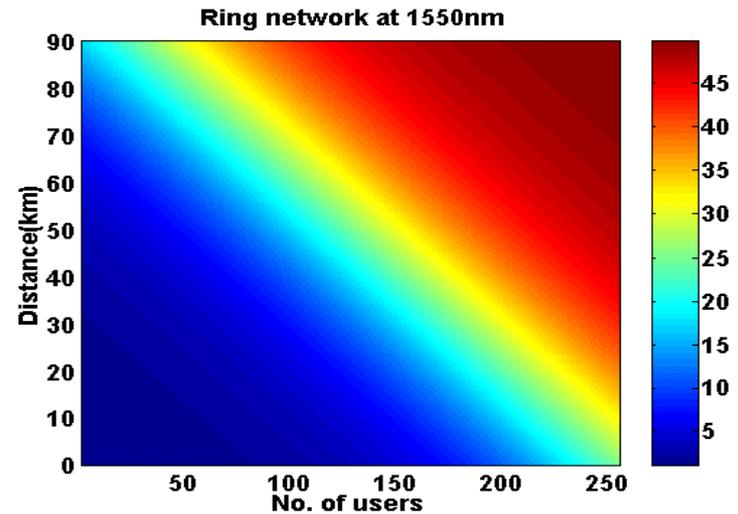
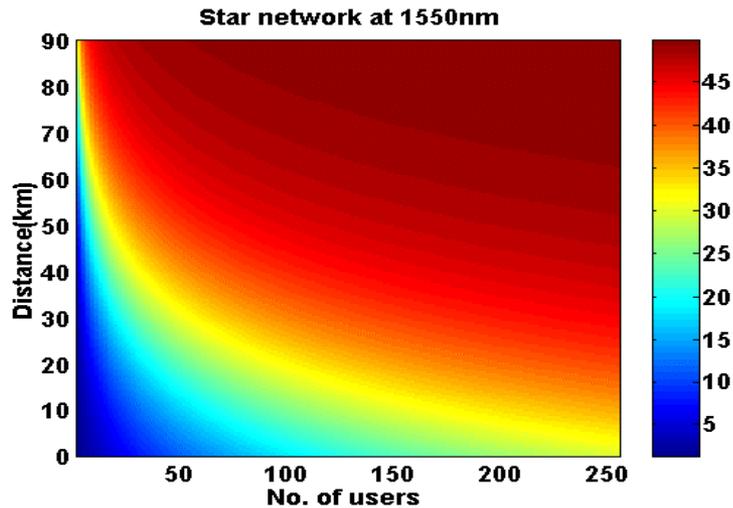
$f$  - repetition frequency

- Network topologies are compared using analysis of their QBER
- High QBER values result in decreased total number of keys available for encrypting data
- Networks with QBER > 15% vulnerable to eavesdropping

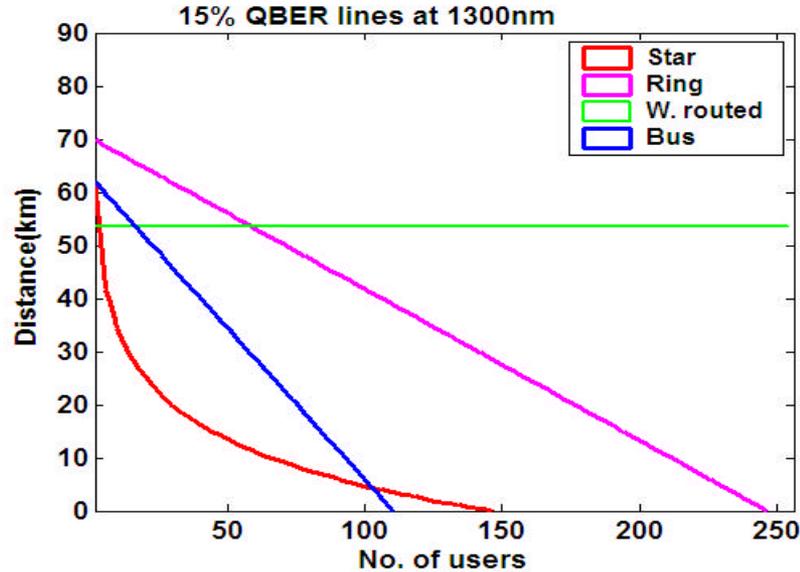
For secure communication, QBER < 15%

*\*“Quantum Cryptography” Nicholas Gisin, Reviews of Modern Physics, January 2002.*

# Comparison of the four networks @ 1550nm



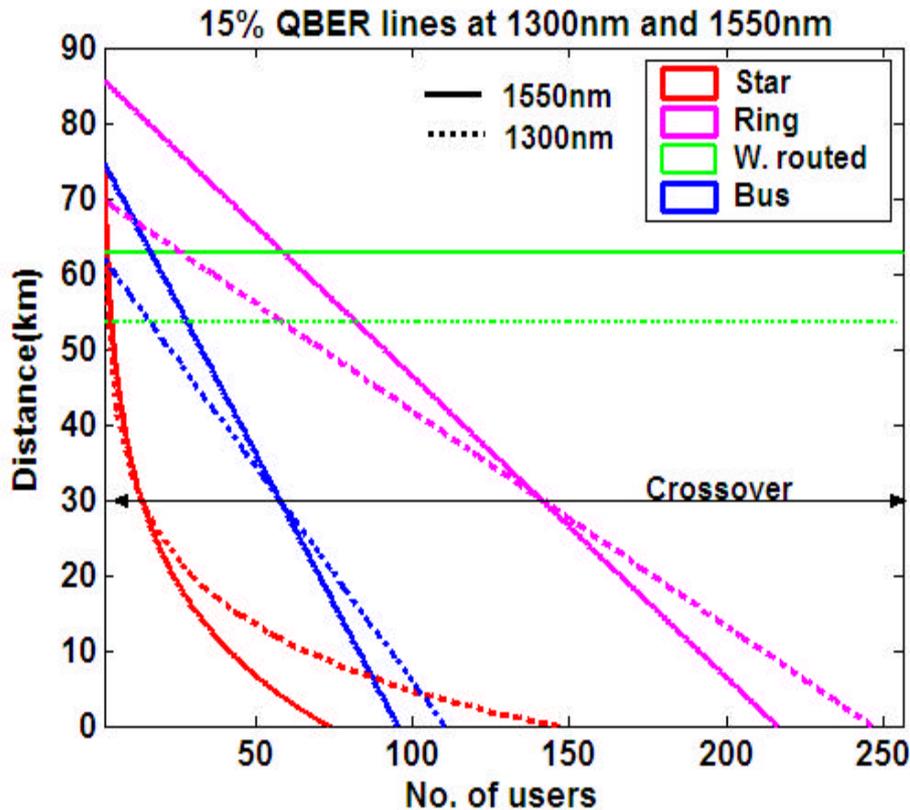
# Comparison of topologies at 1300nm



	<i>Maximum distance for secure communication (km)</i>			
<i>No. of users</i>	<b>Star</b>	<b>Ring</b>	<b>W. routed</b>	<b>Bus</b>
<i>1,2</i>	<b>60,54</b>	<b>70</b>	<b>54</b>	<b>62</b>
<i>3-17</i>	<b>28-54</b>	<b>65-70</b>	<b>54</b>	<b>54-62</b>
<i>18-59</i>	<b>12-28</b>	<b>54-65</b>	<b>54</b>	<b>30-54</b>
<i>60-102</i>	<b>5-12</b>	<b>42-54</b>	<b>54</b>	<b>5-30</b>
<i>103-128</i>	<b>2-5</b>	<b>34-42</b>	<b>54</b>	<b>0-5</b>

**Maximum distance available for secure key distribution with number of users on network**

# Comparison of topologies at 1300nm and 1550nm



Maximum distance for secure communication vs. number of users at wavelengths of 1550nm and 1300nm

- 1300nm and 1550nm lines cross each other at distance of 30km (crossover)
- Distances  $>$  crossover distance  $\Rightarrow$  QKD at 1550nm better
- Distances  $<$  crossover distance  $\Rightarrow$  QKD at 1300 nm better
- For wavelength-routed network, 1300nm and 1550nm lines do not cross each other (parallel lines); QKD at 1550nm is always better than QKD at 1300nm
- This mainly has to do with assumptions in fiber-loss and detector efficiency in the model

# Conclusions

## ✦ Star network

- ✦ 1xN splitter acts as 1/N attenuator and hence not suited for large networks
- ✦ Easy to implement

## ✦ Ring network

- ✦ Definition of “distance” limits actual (point-to-point) distance between users
- ✦ Not affected by phase and polarization fluctuations
- ✦ Easily configured to accommodate more users

## ✦ Wavelength-routed network

- ✦ Size of network limited by AWG bandwidth channel
- ✦ AWG loss approximately uniform with number of wavelength channels and hence number of users on network. Best suited for networks with large users

## ✦ Bus network

- ✦ Grating inserted into network for every user added makes system more lossy and hence not suitable for large networks
  - ✦ Easily configured to accommodate more users
- Acknowledgement

# Conclusions

- ✦ Simulations assumes present COTS device technology
  - ✦ Present work on single photon detector can increase quantum efficiency
  - ✦ Single photon generator, (Number or Fock state generators) can increase mean photon number from  $\mu = 0.1$  to  $\mu = 1$ , adding 10dB margin
- ✦ Theoretical work
  - ✦ Quantum repeaters still theoretical. Many many years until a usable networking device
- ✦ Main interests
  - ✦ Those that require a future proof encryption scheme
    - ✦ **Present state of the art encryption vulnerable to near-future computers capable of peta-flop calculations**
    - ✦ **Adversaries can store data for 10-20 years, until such computers are available**
  - ✦ Financial community
  - ✦ Government and Defense applications
- ✦ Acknowledgement
  - ✦ NSF-ITR and ARO for research funding